

## Department of Mathematics and Humanities

### Ph.D. examination Written Test Syllabus of Mathematics, Management and English

#### Subject: Mathematics

**Calculus:** Functions of two or more variables, continuity, directional derivatives, partial derivatives, total derivative, maxima and minima, saddle point, method of Lagrange's multipliers; Double and Triple integrals and their applications to area, volume and surface area; Vector Calculus: gradient, divergence and curl, Line integrals and Surface integrals, Green's theorem, Stokes' theorem, and Gauss divergence theorem.

**Linear Algebra:** Finite dimensional vector spaces over real or complex fields; Linear transformations and their matrix representations, rank and nullity; systems of linear equations, characteristic polynomial, eigenvalues and eigenvectors, diagonalization, minimal polynomial, Cayley-Hamilton Theorem, Finite dimensional inner product spaces, Gram-Schmidt orthonormalization process, symmetric, skew-symmetric, Hermitian, skew-Hermitian, normal, orthogonal and unitary matrices; diagonalization by a unitary matrix, Jordan canonical form; bilinear and quadratic forms.

**Real Analysis:** Metric spaces, connectedness, compactness, completeness; Sequences and series of functions, uniform convergence, Ascoli-Arzelà theorem; Weierstrass approximation theorem; contraction mapping principle, Power series; Differentiation of functions of several variables, Inverse and Implicit function theorems; Lebesgue measure on the real line, measurable functions; Lebesgue integral, Fatou's lemma, monotone convergence theorem, dominated convergence theorem.

**Complex Analysis:** Functions of a complex variable: continuity, differentiability, analytic functions, harmonic functions; Complex integration: Cauchy's integral theorem and formula; Liouville's theorem, maximum modulus principle, Morera's theorem; zeros and singularities; Power series, radius of convergence, Taylor's series and Laurent's series; Residue theorem and applications for evaluating real integrals; Rouché's theorem, Argument principle, Schwarz lemma; Conformal mappings, Möbius transformations.

**Ordinary Differential equations:** First order ordinary differential equations, existence and uniqueness theorems for initial value problems, linear ordinary differential equations of higher order with constant coefficients; Second order linear ordinary differential equations with variable coefficients; Cauchy-Euler equation, method of Laplace transforms for solving ordinary differential equations, series solutions (power series, Frobenius method); Legendre and Bessel functions and their orthogonal properties; Systems of linear first order ordinary differential equations, Sturm's oscillation and separation theorems, Sturm-Liouville eigenvalue problems, Planar autonomous systems of ordinary differential equations: Stability of stationary points for linear systems with constant coefficients, Linearized stability, Lyapunov functions.

**Algebra:** Groups, subgroups, normal subgroups, quotient groups, homomorphisms, automorphisms; cyclic groups, permutation groups, Group action, Sylow's theorems and their applications; Rings, ideals, prime and maximal ideals, quotient rings, unique factorization domains, Principle ideal domains, Euclidean domains, polynomial rings, Eisenstein's irreducibility criterion; Fields, finite fields, field extensions, algebraic extensions, algebraically closed fields

**Functional Analysis:** Normed linear spaces, Banach spaces, Hahn-Banach theorem, open mapping and closed graph theorems, principle of uniform boundedness; Inner-product spaces, Hilbert spaces,

orthonormal bases, projection theorem, Riesz representation theorem, spectral theorem for compact self-adjoint operators.

Numerical Analysis: Systems of linear equations: Direct methods (Gaussian elimination, LU decomposition, Cholesky factorization), Iterative methods (Gauss-Seidel and Jacobi) and their convergence for diagonally dominant coefficient matrices; Numerical solutions of nonlinear equations: bisection method, secant method, Newton-Raphson method, fixed point iteration; Interpolation: Lagrange and Newton forms of interpolating polynomial, Error in polynomial interpolation of a function; Numerical differentiation and error, Numerical integration: Trapezoidal and Simpson rules, Newton-Cotes integration formulas, composite rules, mathematical errors involved in numerical integration formulae; Numerical solution of initial value problems for ordinary differential equations: Methods of Euler, Runge-Kutta method of order 2.

Partial Differential Equations: Method of characteristics for first order linear and quasilinear partial differential equations; Second order partial differential equations in two independent variables: classification and canonical forms, method of separation of variables for Laplace equation in Cartesian and polar coordinates, heat and wave equations in one space variable; Wave equation: Cauchy problem and d'Alembert formula, domains of dependence and influence, non-homogeneous wave equation; Heat equation: Cauchy problem; Laplace and Fourier transform methods.

Topology: Basic concepts of topology, bases, subbases, subspace topology, order topology, product topology, quotient topology, metric topology, connectedness, compactness, countability and separation axioms, Urysohn's Lemma.

Linear Programming: Linear programming models, convex sets, extreme points; Basic feasible solution, graphical method, simplex method, two phase methods, revised simplex method; Infeasible and unbounded linear programming models, alternate optima; Duality theory, weak duality and strong duality; Balanced and unbalanced transportation problems, Initial basic feasible solution of balanced transportation problems (least cost method, north-west corner rule, Vogel's approximation method); Optimal solution, modified distribution method; Solving assignment problems, Hungarian method.

## **Subject: Management**

### **Unit –I**

Management Concept, Process, Theories and Approaches, Management Roles and Skills

Functions–Planning,Organizing,Staffing,CoordinatingandControlling.Communication–Types, Process and Barriers.

Decision Making– Concept, Process, Techniques and Tools

Organisation Structure and Design – Types, Authority, Responsibility, Centralisation, Decentralisation and Span of Control

Managerial Economics –Concept & Importance

Demand analysis – Utility Analysis, Indifference Curve, Elasticity& Forecasting

Market Structures–Market Classification &Price Determination

National Income – Concept, Types and Measurement

Inflation – Concept, Types and Measurement Business

Ethics& CSR Ethical Issues & Dilemma Corporate

Governance Value Based Organisation

### **Unit–II**

Organisational Behaviour –Significance &Theories

Individual Behaviour–Personality, Perception, Values, Attitude, Learning and Motivation

Group Behaviour – Team Building, Leadership, Group Dynamics

Interpersonal Behaviour & Transactional Analysis

Organizational Culture & Climate

Work Force Diversity & Cross Culture Organisational Behaviour

Emotions and Stress Management

Organisational Justice and Whistle Blowing

Human Resource Management Concept, Perspectives, Influences and Recent Trends

Human Resource Planning, Recruitment and Selection, Induction, Training and Development

Job Analysis, Job Evaluation and Compensation Management

### **Unit–III**

Strategic Role of Human Resource Management

Competency Mapping & Balanced Scoreboard Career

Planning and Development

Performance Management and Appraisal

Organization Development, Change & OD Interventions Talent

Management & Skill Development

Employee Engagement & Work Life Balance

Industrial Relations: Disputes & Grievance Management, Labour Welfare and Social Security

Trade Union & Collective Bargaining

International Human Resource Management – HR Challenge of International Business

Green HRM

### **Unit–IV**

Accounting Principles and Standards, Preparation of Financial Statements

Financial Statement Analysis – Ratio Analysis, Funds Flow and Cash Flow Analysis, DuPont Analysis

Preparation of Cost Sheet, Marginal Costing, Cost Volume Profit Analysis

Standard Costing & Variance Analysis

Financial Management, Concept & Functions

Capital Structure – Theories, Cost of Capital, Sources and Finance Budgeting and

Budgetary Control, Types and Process, Zero base Budgeting

Leverages – Operating, Financial and Combined Leverages, EBIT –

EPS Analysis, Financial Breakeven Point & In difference Level.

### **Unit–V**

Value & Returns – Time Preference for Money, Valuation of Bonds and Shares, Risk and Returns; Capital Budgeting –

Nature of Investment, Evaluation, Comparison of Methods; Risk and Uncertainty Analysis

Dividend – Theories and Determination

Mergers and Acquisition –

Corporate Restructuring, Value Creation, Merger Negotiations, Leveraged Buyouts, Takeover

Portfolio Management – CAPM, APT

Derivatives–Options,OptionPayoffs,OptionPricing,ForwardContracts&Future  
Contracts  
WorkingCapitalManagement–Determinants,Cash,Inventory,ReceivablesandPayables  
Management, Factoring  
International Financial Management, Foreign exchange market

## **Unit-VI**

Strategic Management–Concept, Process, Decision & Types  
StrategicAnalysis–  
ExternalAnalysis,PEST,Porter’sApproachtoindustryanalysis,InternalAnalysis –Resource  
Based Approach, Value Chain Analysis

Strategy Formulation – SWOT Analysis, Corporate Strategy – Growth, Stability,  
Retrenchment, Integration and Diversification, Business Portfolio Analysis - BCG,GE  
Business Model, Ansoff’s Product Market Growth Matrix

StrategyImplementation–ChallengesofChange,DevelopingProgramsMckinsey7s  
Framework

Marketing–Concept,Orientation,TrendsandTasks,CustomerValueandSatisfaction

Market Segmentation, Positioning and Targeting

Product and Pricing Decision – Product Mix, Product Life Cycle, New Product  
development, Pricing –Types and Strategies

Place and promotion decision – Marketing channels and value networks, VMS, IMC,  
Advertising and Sales promotion

## **Unit-VII**

ConsumerandIndustrialBuyingBehaviour:TheoriesandModelsofConsumerBehaviour

BrandManagement–  
RoleofBrands,BrandEquity,EquityModels,DevelopingaBrandingStrategy;BrandName  
Decisions, Brand Extensions and Loyalty

LogisticsandSupplyChainManagement,Drivers,Valuecreation,SupplyChainDesign,Designin  
gandManaging Sales Force, Personal Selling

ServiceMarketing–ManagingServiceQualityandBrands,MarketingStrategiesofService Firms

Customer Relationship Marketing–Relationship Building, Strategies, Values and Process

Retail Marketing– Recent Trends in India, Types of Retail Outlets.

EmergingTrendsinMarketing–Conceptofe-  
Marketing,DirectMarketing,DigitalMarketingandGreen Marketing

International Marketing–Entry Mode Decisions, Planning Marketing Mix for  
International Markets

## **Unit-VIII**

StatisticsforManagement:Concept,MeasuresOfCentralTendencyandDispersion,ProbabilityD  
istribution–Binominal,Poisson,NormalandExponential

Data Collection & Questionnaire Design  
Sampling–Concept, Process and Techniques  
Hypothesis Testing – Procedure; T, Z, F, Chi-square tests  
Correlation and Regression Analysis  
Operations Management–Role and Scope

Facility Location and Layout–Site Selection and Analysis, Layout–Design and Process

Enterprise Resource Planning – ERP Modules, ERP implementation  
Scheduling; Loading, Sequencing and Monitoring  
Quality Management and Statistical Quality Control, Quality Circles, Total Quality Management–  
KAIZEN, Benchmarking, Six Sigma; ISO 9000 Series Standards

Operation Research–Transportation, Queuing Decision Theory, PERT/CPM

## **Unit–IX**

International Business–Managing Business in Globalization Era; Theories of International Trade;  
Balance of payment

Foreign Direct Investment– Benefits and Costs

Multilateral regulation of Trade and Investment under WTO International  
Trade Procedures and Documentation; EXIM  
Policies Role of International Financial Institutions–IMF and World Bank  
Information Technology–Use of Computers in Management Applications; MIS, DSS

Artificial Intelligence and Big Data

Data Warehousing, Data Mining and Knowledge Management – Concepts  
Managing Technological Change

## **Unit –X**

Entrepreneurship Development–  
Concept, Types, Theories and Process, Developing Entrepreneurial Competencies

Intrapreneurship – Concept and Process

Women Entrepreneurship and Rural Entrepreneurship

Innovations in Business–  
Types of Innovations, Creating and Identifying Opportunities, Screening of Business Ideas

Business Plan and Feasibility Analysis–Concept and Process of Technical, Market and Financial  
Analysis

Micro and Small Scale Industries in India; Role of Government in Promoting  
SSI Sickness in Small Industries–Reasons and Rehabilitation  
Institutional Finance to Small Industries–Financial Institutions, Commercial Banks, Cooperative  
Banks, Micro Finance.

**Subject: English**

Indian writing in English

Postcolonial fiction

Literary theory and criticism